Is there the Pareto principle in public library circulation?
A case study of one public library in Taiwan

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ABSTRACT

The Pareto Principle, also known as the 80/20 rule is currently an important and popular management rule applied to marketing and customer relationship management (CRM). The rule indicates that the vital few causes inputs or efforts bringing the most results, outputs, or rewards. Analyzing circulation data to understand the usage status of library collections can help libraries comprehend their patrons' behaviour. However, little research has been done to analyse circulation data of public libraries to reveal patrons' usage behaviours. This paper aimed to analyse the circulation data generated by a municipality public library in Taiwan to gauge if the Pareto Principle manifested in this context. Subsequently, using bibliomining analysis, this research further identified vital patrons and their characteristics, as well as book-borrowed distributions to help analyse patrons' book borrowing behaviour to improve the efficiency of library management and library marketing as well as CRM. The circulation data of the public library follows the Pareto Principle, approximating to the 80/20 rule. Findings showed that when the accumulative percentage of patron is 24.7 percent, the accumulative percentage of borrowed books is 75.3 percent. The vital few patrons borrow the majority of the collections. This paper is the first study to reveal that the Pareto Principle could be found in circulation data of a public library in Taiwan. It could help libraries identify vital patrons and major collections, and improve the efficiency of their management and marketing activities in future. For other types of libraries, it would be interesting for us to explore the existence of the Pareto Principle further.

INTRODUCTION

In recent years, the concept of the Pareto Principle has become a popular guideline or tool in multiple business areas and the social context. The 80/20 rule indicates that there is an unbalanced relationship between causes and results or between efforts and rewards: specifically, it maintains that 80 percent of rewards usually come from 20 percent of efforts, and the other 80 percent of efforts only produce 20 percent of the results. Therefore, if one could recognize, focus on, and control the vital 20 percent of efforts, her or she would obtain greater profits or efficiency. Similarly, if one could reform the 80 percent of effort exerted in vain, he or she would decrease losses. Many natural phenomena have been shown empirically to exhibit such a distribution.

Can the Pareto Principle be applied in the library and information service context? In recent years, a great deal of research has analysed library data and uncovered a variety of trends, patterns, and relationships. Bibliomining, or data mining in libraries, is the application of data mining techniques to data produced from library services (Nicholson 2003; Nicholson 2006; Shieh 2009). By applying statistics, bibliometrics, or data mining tools, libraries can better understand usage patterns and rules, enabling library managers to make decisions to meet user needs based on those mining results (Arsenova 2013; Zhang and Wang 2013; Xiang and Hao 2014; Hajek and Stejskal 2017). However, quality decisions must be based on quality data. Data processing is an important step in the knowledge discovery process (Han, Pei and Kamber 2011; Pandey 2014; Bajpai and Metkewar 2016). Identifying vital data and reducing the data to be analysed can lead to huge decision-making payoffs. Identifying vital patrons and core collections would allow library managers to provide better services.

Examining checkout distributions of circulation data helps libraries understand user behaviours. Previous discussions of data mining applications in academic libraries have emphasized usage analysis (Siguenza-Guzman et al. 2015). There have been a number of studies that have investigated usage analysis of academic libraries (Ahmad, Brogan and Johnstone 2014; Ping 2015; Al-Daihani and Abrahams 2016; Wu, Hu and Wang 2017). Renaud et al. (2015) analysed data from a university library and revealed the distributions of check-out activities based on criteria such as user type, academic department, Library of Congress classification, material type and material life span. They also correlated the findings with student grade point averages. Goodall and Pattern (2011) analysed the usage data of electronic resources, book loans, and visits in an academic library and correlated these data points with academic achievement. However, previous studies have mostly neglected to analyse circulation data in public libraries. In comparison with academic libraries, public libraries provide services to a wide range of users. Before data mining and data analytics,

segmenting these various users and collections would conduct meaningful results. At present research focusing on this issue is still uncommon.

This study aims to discern if there are vital few patrons who borrow most of the collection, and to identify the vital patrons and their characteristics and book-borrowed distributions. Specifically, the objective of this study is to analyse the circulation data of public libraries and to examine whether the phenomenon of Pareto Principle could be found. If the Pareto Principle as conceptualized for this study could, in fact, be used to study patron patterns, this rule can serve as a much needed tool for public libraries to target patrons and effectively market their services. In view of the objective outlined above, three research questions are posed:

(a) Does the phenomenon of Pareto Principle manifest in the circulation data of public libraries? What is the percentage breakdown?

(b) Applying the 80/20 rule, what are the characteristics of the top 20 percent vital patrons?

(c) Applying the 80/20 rule, what are the characteristics of the collections borrowed by the top 20 percent vital patrons?

LITERATURE REVIEW

The 80/20 rule originated from the Pareto Principle, named after the Italian economist Vilfredo Pareto who identified a general imbalance in property allocation: most (80%) wealth belongs to a few (20%) people. This model of imbalance has been observed repeatedly (Koch 1998; Nash 2016). In 1941, management consultant Joseph M. Juran applied this principle to quality management issues. He believed the principle of "the vital few and the trivial many" was universal (Koch 1998). In the late 1940s, Juran named his notion of "the vital few and the trivial many" as Pareto Principle after the Italian economist. The 80/20 rule is an extension of the Pareto Principle developed by Richard Koch based on a theoretical view of Pareto and Juran, which he publicized in "*The 80/20 Rule Principle – The Secret of Achieving More with Less.*" Koch (1998) noted that few causes, inputs, or efforts could bring most results, outputs, or rewards. The 80/20 rule indicates that there is always an imbalance between causes and results, between inputs and outputs, or between efforts and rewards. The relationship between 80 percent and 20 percent provides a credible point of this phenomenon of imbalance: generally, 80 percent of outputs come from 20 percent inputs; 80 percent of results come from 20 percent of causes; and 80 percent of achievements come from 20 percent of efforts.

Koch (1998) pointed out that the 80/20 rule could be applied in either the business or social context and in various fields. For example In business, 80 percent of a company's profits come from 20 percent of its customers, 80 percent of revenues come from 20 percent of the products, and 80 percent of sales come from 20 percent of the sellers (Koch 1998; Kim, Singh and Winer 2017). In quality management, 80 percent of the problems come from 20 percent of the faults (Koch 1998). In computer science, most software takes 80 percent of the time to run 20 percent of the programs (Koch 1998; Yamashita et al. 2015). In society, 80 percent of the crimes are 20 percent of the crimes behaviours, and 20 percent of drivers cause 80 percent of traffic accidents (Koch 1998). The unbalanced relationship between efforts and rewards or causes and results makes delineating the vital few very important. A successful company uses less effort to achieve high profits. Companies may improve profitability by reducing outputs or unbalancing employee salaries. To achieve this goal, they must identify which employees, departments, or units produce the most profits and provide them more resources, because concentrating on the groups of customers and the specific markets that are profitable can substantially improve a company's bottom line, having insight into the vital few is an important issue. Several studies also have suggested the benefit of applying the 80/20 rule (Yamashita et al. 2015; Kim et al. 2017; Mesbahi, Rahmani and Hosseinzadeh 2017).

The study of the Pareto Principle in libraries was initialized by Trueswell (1969) who applied the 80/20 rule to address the relationship between library collections and circulation numbers. Trueswell (1969) noted that about 20 percent of collections bring 80 percent of circulation numbers (Nash 2016). Hardesty (1981) traced the book acquisitions and circulations of a university for five years. He found that 30 percent of books accounted for 80 percent of circulation. In recent years, Singson and Hangsing (2013; 2015) analysed usage patterns of electronic journals academic consortia. They found out that the user downloads for some publishers follow the 80/20 rule. The few core journals were downloaded the most. Some research suggested the 80/20 rule could be used to identify the core collections within libraries. Burrell (1985) investigated the circulation data of university libraries and public libraries and found between 43 to 58 percent of circulating collections are required to account for 80 percent of borrowings. He developed a theoretical model of library operations to help libraries identify their core collections. Nisonger (2008) examined the 80/20 rule in relation to the use of print serials, downloads from electronic databases, and journal citations, concluding that the 80/20 rule is a valid method for determining core concepts in journal collection management. However, few previous studies have explored the distributions of circulation in public libraries. This study examines a circulation dataset from a public library in Taiwan and analyses usage patterns to understand the distributions of patrons and circulations. The purpose is to identify if there are vital patrons in public libraries.

This study concerns with the marketing of libraries and thus mainly examines the Pareto Principle based on the patrons' viewpoint.

MATERIALS AND METHOD

A public library in Taiwan is chosen as the case setting; it is located in a developing city that has a large area and fast-growing population. There are approximately 30 districts in the city, each district owns at least one library branch. The main library is located in the same district with the city government, and there are more than 100 library branches and reading rooms over the whole city. Reading rooms are small branches with smaller scale, which can serve in various regions and touch different kinds of people.

There are four types of data used in this study and they come from the following dataset:

(a) Circulation data: This dataset contains more than 18 million transactions conducted over two years and includes patron ID, item ID, branch library name, and date of transaction. Transaction types include local-borrow transactions, inter-borrow transactions and reservations.

(b) Patron data: This dataset contains data about 460,000 patrons, including patron ID, patron type, name of patron's branch library, and patron gender and occupation.

(c) Item data: This dataset encompasses all lending items in the public library, including item ID, title, author, call number, material type, subject code, and the name of the branch library that houses the item.

(d) Location data: This dataset contains information about each branch library such as branch name and district.

To preserve data privacy, the data went through pre-processing before they were obtained and processed by the researchers. The data used for data mining were first processed with one-way hashing function by the library (the raw data owner) and then the subset data were provided for the study. Columns that may have identified someone by providing information such as patron names, addresses, or phone numbers were deleted. Furthermore, patron corresponding data and branch names had been translated into substituted codes by some one-way hash functions respectively (Schneier 2015).

This paper analyses public library data to determine if the 80/20 phenomenon of Pareto Principle manifests in libraries, and then identifies the distributions of the patrons and circulations. The data processing procedures involve the following:

(a) Integrating circulation data: The local-borrow transactions, inter-borrow transactions, and reservation data are integtated into one table.

(b) Ranking the patrons: The transactions for each patron ID are summed up and then ranked in the table by the number of transaction.

(c) Calculating the accumulative percentage: The accumulative total of patrons and the accumulative total of items are calculated; the accumulative percentage are calculated separately. The accumulative percentage of patrons is the patron percentage rank divided by the total number of patrons. The accumulative percentage of items is the percentage of the accumulative total of that item divided by total number of items.

(d) Examining the circulation data with the Pareto Principle: The datum where the accumulative percentage of patrons and the accumulative percentage of items is 100% is identified. In addition to the total data from the two years, the data for each year are examined separately to identify the percentage with the concept of Pareto Principle in each year.

(e) Analyzing the distributions of circulation data: After identifying the percentage, the concept of 80/20 rule is used to further analyse the distributions of circulation. The analysis involves collections borrowed by the top 20 percent of active patrons and considers the features of these collections such as subject, and material type. The analysis also takes in the patrons who borrowed 80 percent of items in the leaderboard and considers the characteristics of these patrons such as gender, occupation, and districts.

The database system used in this study is Microsoft SQL Server 2014. The data mining and analysis tools used are Microsoft SQL Server Data Tools (SSDT) and Microsoft Excel 2016 respectively. The researchers adopted a PC workstation with Intel Core i7-7700 CPU, 16G memory and 1T SSD to support database system operation, data processing and analysis tasks.

RESULTS AND DISCUSSIONS

The Pareto Principle

The patrons are ranked according to the number of items they borrow and the following are calculated – the accumulative total of patrons, the accumulative total of items, the accumulative total percentage of patrons, and the accumulative total percentage of items. As shown in Table 1, when the accumulative percentage of patrons is 24.69 percent, the accumulative percentage of items is 75.31 percent. That the accumulative percentage of patrons and the accumulative percentage of items is 100 percent demonstrates that the circulation data of the public library follow the Pareto Principle approximating to 80/20 rule. In other words, the vital few patrons account for most of the borrowings. The data in which

the accumulative percentage of patrons is 20 percent and the accumulative percentage of items is 80 percent are also shown in Table 1.

Table 1: Rank of Borrowing and Accumulative Percentage

Borrow Amount	Accumulative patrons	Accumulative items	Accumulative patrons(%)	Accumulative items(%)
3212	1	3212	0.000217507	0.017778698
3159	2	6371	0.000435013	0.035264036
3088	3	9459	0.00065252	0.052356383
3030	4	12489	0.000870027	0.069127695
2990	5	15479	0.001087533	0.085677604
2973	6	18452	0.00130504	0.102133416
≈				
56	91950	12534661	19.99973899	69.38043286
56	91951	12534717	19.9999565	69.38074283
56	91952	12534773	20.00017401	69.38105279
56	91953	12534829	20.00039151	69.38136275
≈				
44	113496	13606589	24.68613786	75.31364706
44	113497	13606633	24.68635537	75.3138906
44	113498	13606677	24.68657288	75.31413415
44	113499	13606721	24.68679038	75.31437769
≈				
35	134910	14453189	29.34382586	79.99965129
35	134911	14453224	29.34404336	79.99984502
35	134912	14453259	29.34426087	80.00003875
35	134913	14453294	29.34447838	80.00023247
≈				

This study also analyses the data for each year separately (Table 2). For the first year, when the accumulative percentage of patrons is 26.76 percent, the accumulative percentage of items is 73.24 percent, and the sum of these two percentages is 100 percent. For the second year, when the accumulative percentage of patrons is 26.17 percent, the accumulative percentage of items is 73.83 percent, and the sum of these two percentages is 100 percent. Although the percentage is a little different in each year, they can be explained by the 80/20 rule. Overall, the findings indicate that the circulation data of public libraries adhere to the Pareto Principle.

In summary, the percentage following the 80/20 rule for the two years examined is 75.3/24.7. For the first year and the second year, the percentages are 73/27 and 74/26 separately. These findings indicate that a few patrons would borrow the most items in the public library. The application of 80/20 rule to identify the vital few patrons can significantly improve organizational efficiency, and the public library managers would certainly benefit from embracing this approach. In doing so, they could not only improve utilization but also give vital patrons more proper services.

Table 2: Rank of Borrowing and Accumulative Percentage of Each Year

	First Year					Second Year			
Borrow Amount	Accumulative patrons	Accumulative items	Accumulative patrons(%)	Accumulative items(%)	Borrow Amount	Accumulative patrons	Accumulative items	Accumulative patrons(%)	Accumulative items(%)
3212	1	3212	0.000302	0.039732	2386	1	2386	0.000295	0.023902
3159	2	6371	0.000605	0.078808	2048	2	4434	0.000591	0.044418
3030	3	9401	0.000907	0.116288	1605	3	6039	0.000886	0.060497
2973	4	12374	0.001209	0.153064	1346	4	7385	0.001182	0.073981
2119	5	14493	0.001511	0.179275	1328	5	8713	0.001477	0.087284
2013	6	16506	0.001814	0.204176	1328	6	10041	0.001773	0.100588
≈					≈				
36	66166	5226147	19.99952	64.64627	43	67681	6588491	19.99953	66.00144
36	66167	5226183	19.99982	64.64672	43	67682	6588534	19.99982	66.00187
36	66168	5226219	20.00012	64.64716	43	67683	6588577	20.00012	66.0023
36	66169	5226255	20.00042	64.64761	43	67684	6588620	20.00041	66.00273
≈					≈				
27	88518	5921206	26.75569	73.244	32	88568	7369750	26.17157	73.82784
27	88519	5921233	26.756	73.24433	32	88569	7369782	26.17187	73.82816
27	88520	5921260	26.7563	73.24467	32	88570	7369814	26.17216	73.82848
27	88521	5921287	26.7566	73.245	32	88571	7369846	26.17246	73.8288
≈					≈				

The Top 24.7 Percent Patrons

(a) Statistical Analysis of Patrons

After establishing that public library data conform to the 80/20 rule, the distributions of patrons are analysed to determine the characteristics of the top 20 percent active patrons and the features of the 80 percent collections they borrowed from. The two-year dataset for the Taiwan public library includes about 460,000 patrons who borrowed at least one item. Therefore, the top 24.7 percent is composed of about 115,000 patrons who borrowed at least 44 items. Applying the 80/20 rule, these patrons are active users of the library. Identifying and understanding these patrons may help the library target users and market library services to them efficiently.

The characteristics of these top 24.7 percent of patrons are analysed. Table 3 presents the distributions of the top 24.7 percent of patrons by their birth year and gender. In general,

most of the patrons were born in the 1970s, followed by the 2000s, and the percentage of female patrons is higher than that of males. Table 4 shows the results of the distributions of the top 24.7 percent of patrons by types and occupations. Most of the top patrons are general patrons, followed by families. By occupation, students borrow the most, followed by businesses and finance and then children. This is consistent with the findings in the next stage of analysis: families and children are vital patrons and children's books are also a popular material type. For public libraries, categorizing patrons is important because it enables them to develop collections for specific patrons, and recommend specific collections to targeted patrons.

Table 3: Distribution of Patrons' Birth Year and Gender

Year of birth	Female	Male	Not identified
2010s	1156	1126	19
2000s	12690	10544	67
1990s	7693	3713	23
1980s	10693	4254	131
1970s	24498	8749	334
1960s	12083	6748	88
1950s	3769	3424	17
1940s	873	1217	4
1930s	183	327	2
1920s	41	113	1
1910s	10	5	0
Other	82	47	3

Moreover, the top 24.7 percent patrons' percentage by patron type and gender among all patrons are analysed (Table 5). Except for general patrons, other types of patrons have percentages higher than 24.7 percent. Staff has the highest percentage (83%) and VIP patrons (66%) are also vital patrons. By gender, 25.5 percent female patrons and 24 percent male are vital patrons. Females have little higher percentage than the males.

Table 4: Distribution of Patrons' Occupation and Type

Occupation	VIP	General	Volunteer	Family	Group	Staff
Agriculture	2	424	1	-	-	-
Arts	-	-	-	1	-	-
Business and Finance	64	18366	66	52	-	11
Children	91	18009	1	1	-	-
Education and Training	31	4885	29	7	8	2
Entertainment	-	2	-	-	-	-
Fishery	-	3	-	-	-	-
Freelance	-	16	-	4	-	1
General Services	1	16	-	11	-	16
Government	23	5093	23	15	13	261
Healthcare	-	3	-	1	-	-
Homemaker	-	39	-	34	-	-
Industrial	28	7608	14	14	1	1
Military	-	87	-	1	-	-
Others	164	31263	449	186	20	110
Animal agriculture	-	1	-	-	-	-
Religion	-	2	-	-	-	-
Student	113	24905	30	10	-	9
Transportation	-	-	-	1	-	-
Public Servant	-	1	-	-	-	-
Not identified	8	1355	2	710	3	5

Table 5: Percentage of Patrons' Type and Gender.

	Top 24.7% Patrons	Percentage (%)
Patron Type		
VIP Patron	525	66.28788
General Patron	112078	24.6394
Volunteer	615	50.49261
Family	1048	46.41275
Group	45	39.13043
Staff	416	83.36673
Gender		
Female	73771	25.54866
Male	40267	24.03182
Not identified	689	36.63764

(b) Bibliomining Analysis of Patrons

To know the characteristics of these patrons, clustering of data mining techniques are applied to these 24.7 percent patrons. They are divided into four groups by K-means algorithm. Input variables are ages, occupations, and gender. The results are shown in Table 6. Patrons in Cluster 1 are 0-20 years old, they are students or children, comprising 45 percent males and 55 percent females. Approximately 84 percent patrons in Cluster 2 are from 21-32 years old; predominantly students and females. Patrons in Cluster 3 are highly females, mostly from 33-43 years old, and come from business and finance occupation sector. Patrons in Cluster 4 are mainly from 44-81 years old. They are are mainly from business and finance, as well as industries.

Table 6: Clusters of Patrons.

Cluster	Variable	Value	Percentage
Cluster 1	Patron Age	0 - 20	98.88%
	Patron Gender	Female	55.02%
		Male	44.91%
	Patron Occupation	Children	64.13%
		Student	35.23%
Cluster 2	Patron Age	0 - 20	11.35%
		21 - 32	84.47%
		33 - 43	4.19%
	Patron Gender	Female	68.83%
		Male	30.76%
	Patron Occupation	Business and Finance	9.00%
		Children	2.43%
		Education and Training	2.53%
		Government	3.88%
		Industrial	3.32%
		Others	16.61%
		Student	61.94%
Cluster 3	Patron Age	21 - 32	15.01%
		33 - 43	84.99%
	Patron Gender	Female	73.46%
		Male	25.44%
		Null	1.10%
	Patron Occupation	Business and Finance	24.12%
		Education and Training	6.66%
		Government	5.69%
		Industrial	8.60%
		Others	36.11%
		Student	18.21%
Cluster 4	Patron Age	0 - 20	0.62%
		21 - 32	9.33%
		33 - 43	37.25%
		44 - 81	52.80%
	Patron Gender	Female	66.33%
		Male	33.30%
	Patron Occupation	Agriculture	0.72%
		Business and Finance	27.19%
		Education and Training	7.99%
		Government	8.43%
		Industrial	10.40%
		Others	41.75%
		Student	3.38%

The same clustering method was applied to all patrons who borrowed at least one item. The list of clustering results in Table 7 shows a great difference when compared with the previous results in Table 6, indicating that using 20/80 rule could point out the vital patrons.

Table 7: Clusters of All Patrons

Cluster	Variable	Value	Percentage
Cluster 1	Patron Age	0 - 19	100.00%
	Patron Gender	Female	53.85%
		Male	46.07%
	Patron Occupation	Children	52.52%
		Student	47.08%
Cluster 2	Patron Age	0 - 19	100.00%
	Patron Gender	Female	48.09%
		Male	51.85%
	Patron Occupation	Children	98.57%
		Student	0.82%
Cluster 3	Patron Age	0 - 19	74.08%
		20 - 30	25.92%
	Patron Gender	Female	63.23%
		Male	36.70%
	Patron Occupation	Children	15.10%
		Others	0.96%
		Student	82.91%
Cluster 4	Patron Age	0 - 19	3.24%
		20 - 30	16.55%
		31 - 41	36.10%
		42 - 78	44.10%
	Patron Gender	Female	65.17%
		Male	34.40%
	Patron Occupation	Business and Finance	24.05%
		Education and Training	6.77%
		Government	7.77%
		Industrial	9.08%
		Others	37.30%
		Student	14.21%

The Collections Borrowed by the Vital Users

(a) Statistical Analysis of Collections Borrowed

Finally, the features of 75.3 percent collections borrowed by the top 24.7% patrons was analysed. Table 8 shows the materials' types and subject codes in the New Classification Scheme for Chinese Libraries used for general collections. As expected, Chinese books are borrowed most frequently, followed by children's books and the CDs attached to items. In collections organised according to the New Classification Scheme for Chinese Libraries, items belonging to Linguistics and Literature (800) are borrowed most frequently, followed by Applied Sciences (400) and then Arts (900).

Table 8. Distribution of Material Types and Subject Code in New Classification Scheme for Chinese Libraries*

Materials type	000	100	200	300	400	500	600	700	800	900
Chinese Book	43020	353972	140993	242366	1239097	568368	82593	416972	3735515	322321
Foreign Reference	-	-	-	-	4	2	2	-	30	-
Indonesian Book	1	5	2	-	-	1	7	14	31	1
Audio Book	298	4449	686	320	613	1285	-	61	4022	595
English Book	109	376	130	287	68	98	223	791	10929	272
Foreign Child Book	240	256	106	2233	607	5530	714	1079	87368	1109
Infant Book	107	29	-	1605	3291	81781	5	24	32558	295
Child Book	44093	38286	9240	407991	57602	221949	37738	152550	2744094	132242
Child Reference	311	-	-	218	15	43	4	23	102	1
Child Picture Book	-	-	-	-	7	-	-	-	-	-
Attachment	16724	5948	3010	65333	50334	43420	5902	12690	335886	35293
Teeanger Book	-	-	-	-	-	-	-	1	136	-
Goverment Publication	-	-	-	11	116	149	2	43	24	37
Music	4	25	65	-	12	65	-	-	2926	4443
Aboriginal Book	-	-	-	-	-	2	-	-	-	-
Book Box	-	-	-	-	-	-	-	-	95	1
Thai Book	-	-	-	-	-	1	-	-	4	-
Malay Book	2	-	-	-	-	-	2	-	-	-
Reference Book	31	1	14	220	69	109	13	97	95	53
Periodical	51530	737	535	10324	39142	25130	63	1377	16835	8957
Video	713	995	618	12136	5300	7021	2038	8646	7172	353248
Vietnam Book	-	4	-	-	-	-	133	3	47	10
Local Government Literature	3	-	-	5	2	6	4	21	1	4
E-resources	-	-	-	-	-	-	-	-	4	-
Comic Book	2	307	225	635	527	538	176	573	4469	449478
Elderly Book	-	-	-	-	-	-	-	12	5	-
Journal	-	-	10	-	10	1	-	-	-	-
Korean Book	-	-	-	3	1	-	-	-	-	1

*000 Generalities; 100 Philosophy; 200 Religion; 300 Science; 400 Applied Sciences;

500 Social Sciences; 600 History; 700 Geography; 800 Linguistics and Literature; 900 Arts.

In the second layer classification of items that had been borrowed by vital patrons, items belonging to Various Chinese literature (850) are borrowed most frequently, followed by Western literature (870) and then Oriental literature (860). Table 9 shows the distributions of popular items in the second layer classification. In the third layer classification, items borrowed more than 100,000 times belong to Fiction (857), Chinese Children literature (859), Japanese literature (861), and American literature (874). Table 10 shows the top 30 in the third layer classification and the number of items borrowed.

Table 9: Distribution of the Second Layer in New Classification Scheme for Chinese Libraries

000	Items	200	Items	400	Items	600	Items	800	Items
000	1034	200	1451	400	4024	600	2155	800	513959
010	24583	210	8002	410	354624	610	39812	810	108177
020	3650	220	52107	420	659441	620	41626	820	7048
030	1558	230	956	430	74932	630	3225	830	24052
040	32984	240	13626	440	59227	640	299	840	7249
050	55580	250	416	450	653	650	240	850	3509721
060	3896	260	758	460	22872	660	1153	860	1079394
070	8153	270	8502	470	14286	670	30293	870	1505767
080	25382	280	6003	480	30237	680	2444	880	167646
090	209	290	63625	490	175927	690	7794	890	1719
100	Items	300	Items	500	Items	700	Items	900	Items
100	2614	300	253520	500	6347	700	-	900	22963
110	587	310	227258	510	3455	710	79355	910	51115
120	26545	320	27959	520	481670	720	1997	920	13699
130	1339	330	13952	530	45362	730	237834	930	2986
140	5762	340	9745	540	100911	740	71948	940	618495
150	1738	350	28825	550	64512	750	15981	950	47354
160	630	360	30272	560	187592	760	14403	960	44995
170	248746	370	14299	570	19393	770	12993	970	29489
180	5619	380	109185	580	26303	780	148697	980	372912
190	111469	390	26779	590	17938	790	10141	990	103609

Table 10: The Top 30 Third Layer in New Classification Scheme for Chinese Libraries

Classification No.	Items	Classification No.	Items	Classification No.	Items
857	1911334	523	270695	494	108243
859	1276528	855	268203	862	105689
861	921509	312	178680	733	96751
874	677247	563	160722	803	84554
947	577836	177	147883	731	81030
805	370272	528	142726	307	79950
427	337461	411	141158	815	78603
987	332690	876	131703	428	63625
873	313536	308	120121	192	63185
872	288577	426	109827	875	59440

(b) Bibliomining Analysis of Collections Borrowed

The association rules of data mining techniques were applied to the collections borrowed by 24.7 percent patrons, using the second classification number as bases to see the association patterns. Taking one association rule for example, "820,690→850" has the highest confidence, i.e. 0.996. That means, among the vital patrons who had borrowed books of classification number 820 (Chinese literature) and 690 (Chinese travels), 99.6 percent of them also borrowed books of classification number 850 (Various Chinese literature).

CONCLUSION

This paper examines the circulation data of a public library through the lens of the Pareto Principle, finding that the Pareto Principle does manifest in its circulation data. The findings indicate that, during the two-years covered by the investigation, 24.7 percent of the patrons borrowed 75.3 percent of all items borrowed. Conforming to the Pareto Principle, the majority of books-orrowing was done by the vital few patrons. The researchers analysed the distributions of the vital few patrons and the collections most frequently borrowed from. Among the vital few patrons, most of them are students, families, and children. Among the popular collections, the most frequently borrowed items are Chinese books and children's books. The most popular subject collection borrowed is Linguistics and Literature. This study also analysed these patrons and collections by data mining techniques. The findings of clustering have implications for public libraries to understand their patrons. Libraries could apply the Pareto Principle to identify vital patrons and collections and use that information to improve the efficiency of their library service, management and marketing.

Future research should analyse the correlation or connection between the vital few patrons and popular collections. Further studies exploring Pareto Principle based on the circulation data to identify popular items in public libraries could be conducted. The results of such an analysis would enable public librarians to make more effective management and marketing decisions, subsequently helping libraries improve utilization and patron satisfaction and develop collections that are more appealing to their patrons.

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